



# ***Lists***



**Alessandro SAVINO**  
**Politecnico di Torino (Italy)**

*alessandro.savino@polito.it*

*www.testgroup.polito.it*

# *License Information*

**This work is licensed under the  
Creative Commons BY-NC  
License**



To view a copy of the license, visit:

<http://creativecommons.org/licenses/by-nc/3.0/legalcode>

# ***Disclaimer***

- **We disclaim any warranties or representations as to the accuracy or completeness of this material.**
- **Materials are provided “as is” without warranty of any kind, either express or implied, including without limitation, warranties of merchantability, fitness for a particular purpose, and non-infringement.**
- **Under no circumstances shall we be liable for any loss, damage, liability or expense incurred or suffered which is claimed to have resulted from use of this material.**

# ***Goal***

- This lecture aims at presenting Lists as ADT, focusing first on some typical operations and then on possible implementation.**

# ***Prerequisites***

- **Lectures:**
  - **11\_8.1 and 11\_8.2**

## ***Further readings***

- **Students interested in a deeper look at the covered topics can refer, for instance, to the books listed at the end of the lecture.**

# ***Outline***

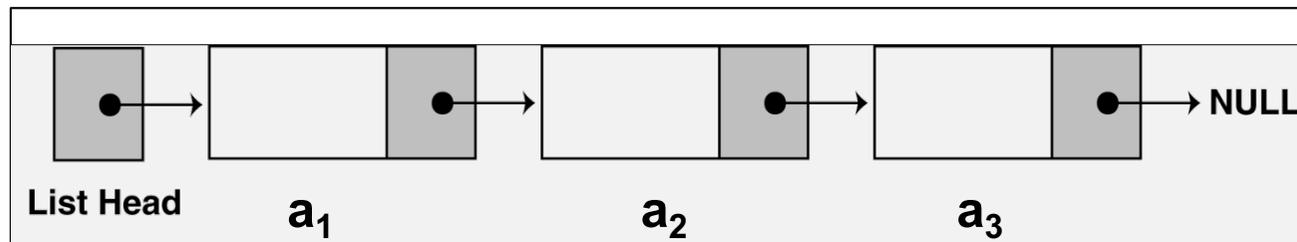
- **Lists**
- **List operations**
- **List implementation**
- **Sentinels**
- **Doubly and multiple linked lists**
- **STL Lists**

# ***Outline***

- Lists**
- List operations**
- List implementation**
- Sentinels**
- Doubly and multiple linked lists**
- STL Lists**

# Liste

- Lists are flexible ADTs
  - A list is a series of connected nodes, where each node is a data structure containing specific information
    - $a_1, a_2, \dots, a_n \quad n \geq 0$
  - It is possible to insert, search, and delete every node inside the list
  - A list can grow or shrink in size as the program runs.



# Definitions

- If  $n = 0$  *empty list*
- $a_1$  first element of the list, or *head*
- $a_n$  the last element of the list, or *tail*
- $a_i$  *precedes*  $a_{i+1}$   $i : 1 \leq i < n$
- $a_i$  *follows*  $a_{i-1}$   $i : 1 < i \leq n$
- Node  $a_i$  is placed in the *position i*

# Definitions

- If  $n = 0$  *empty list*
- $a_1$  first element of the list, or *head*
- $a_n$  the last element of the list, or *tail*
- $a_i$  *precedes*  $a_{i+1}$   $i : 1 \leq i < n$
- $a_i$  *follows*  $a_{i-1}$   $i : 1 < i \leq n$
- Node  $a_i$  is placed in the *position*  $i$

Element or node *position* depends on the actual context and structure implementation, i.e., it may represent an index, address, pointer, or iterator

# ***Outline***

- **Lists**
- **List operations**
- **List implementation**
- **Sentinels**
- **Doubly and multiple linked lists**
- **STL Lists**

## ***insert (x, p, L)***

**Inserts in the list  $L$  an element  $x$  in position  $p$ .**

**Returns:**

- **OK if everything is ok**
- **ERROR otherwise.**



## ***delete (p, L)***

**Deletes in the list  $L$  the element in position  $p$ .**

**Returns:**

- **OK if everything is ok**
- **ERROR otherwise.**



## ***locate* ( $x$ , $p$ , $L$ )**

**Returns the position in the list  $L$  of the first occurrence of  $x$  after position  $p$ .**

**If the element does not exist returns the last element in the list.**



## ***retrieve (p, L)***

**Returns the element of the list L at position p;  
If the element does not exist returns ERROR.**



***next (p, L)***  
***previous (p, L)***

**Return the next or previous position  
of the element in position  $p$ .  
If  $p \notin [1, n]$ , ERROR**



***next (p, L)***  
***previous (p, L)***

**next(n,L) = eol(L)**  
**next(eol(L),L) = ERROR**  
**previous(1,L) = ERROR**



***clear(L)***

**Clear the content of the list.**



## ***first (L)***

**Returns the first position in the list.**



***end(L)***

**Returns the last position in the list.**



# ***Outline***

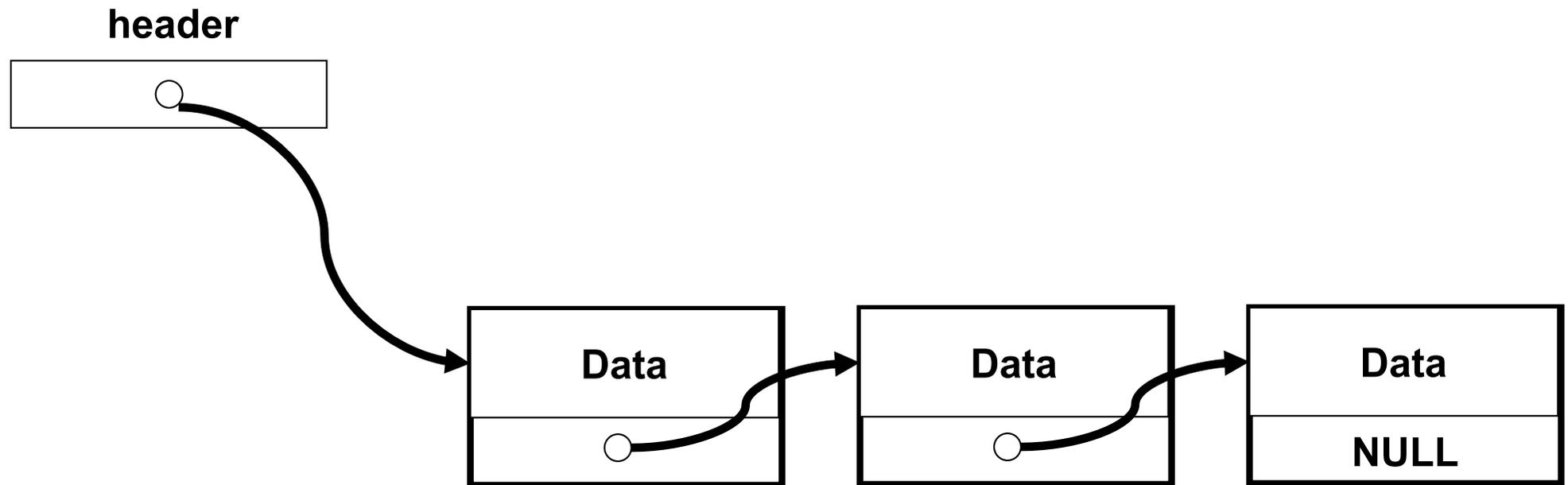
- **Lists**
- **List operations**
- **List implementation**
- **Sentinels**
- **Doubly and multiple linked lists**
- **STL Lists**

# ***List implementation***

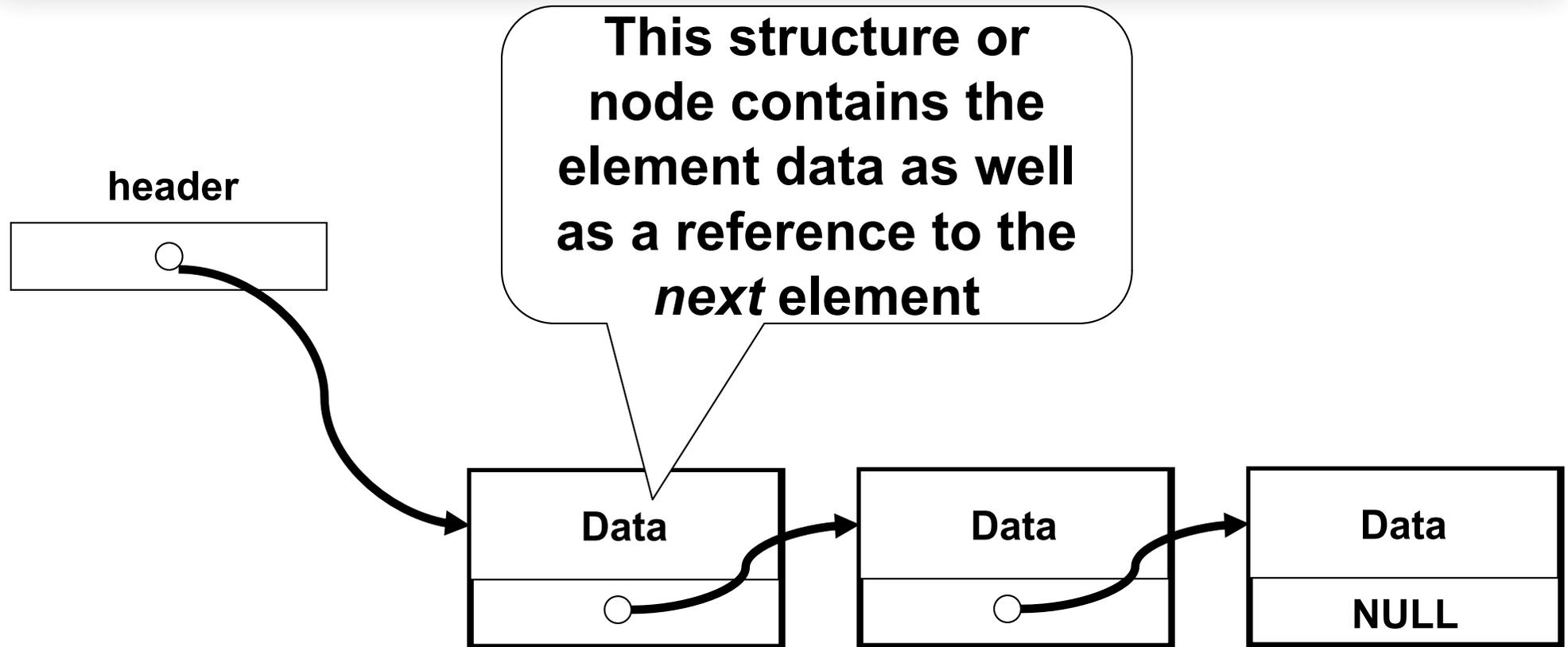
**There are different implementations of a list:**

- **Implicit**
  - **Using vectors**
- **Explicit:**
  - **Devoted structures**
  
- **Implementation may depend on the list operations, list size, programming language.**

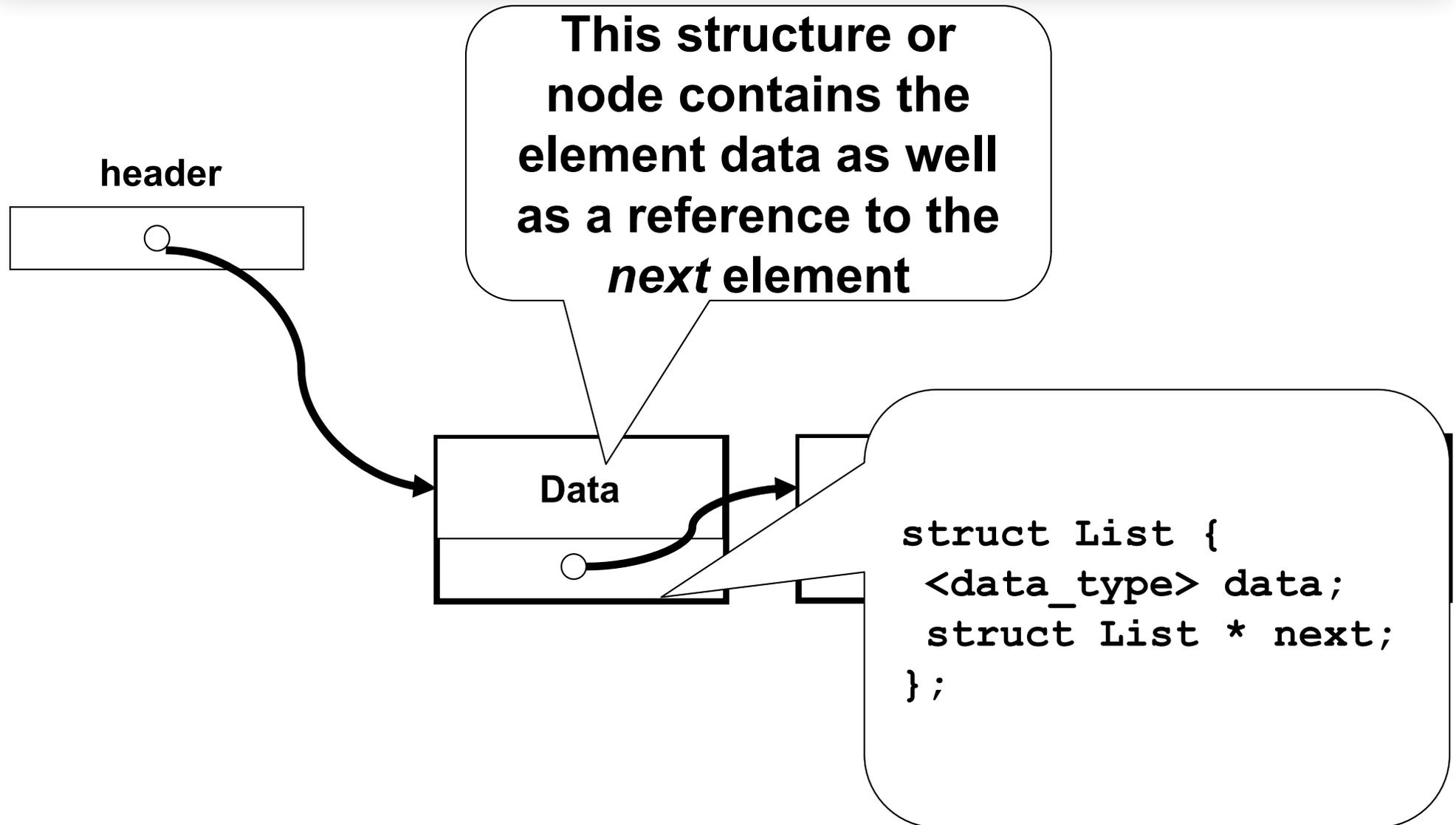
# *List Implementation*



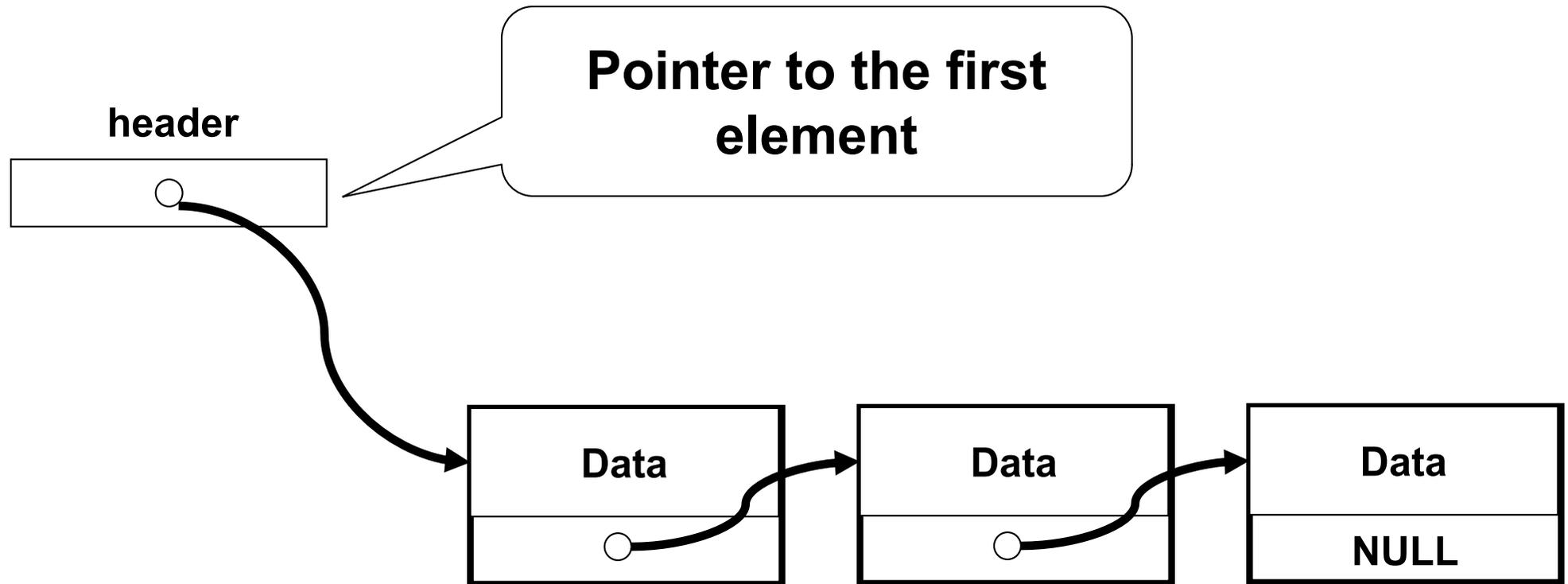
# List Implementation



# List Implementation



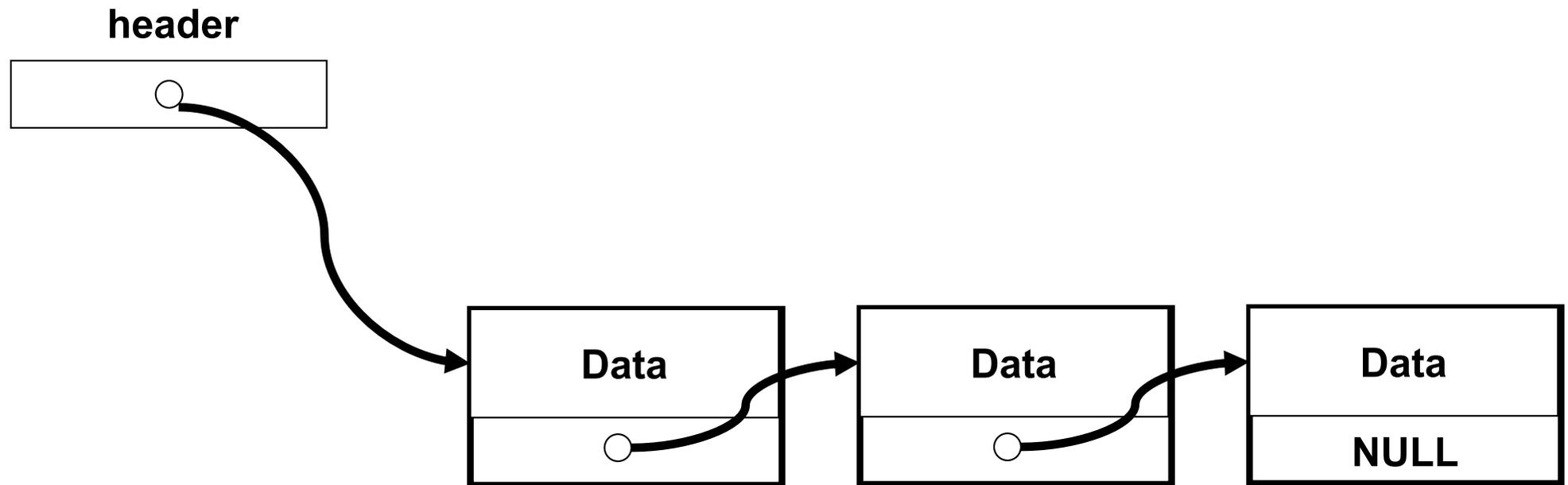
# List Implementation



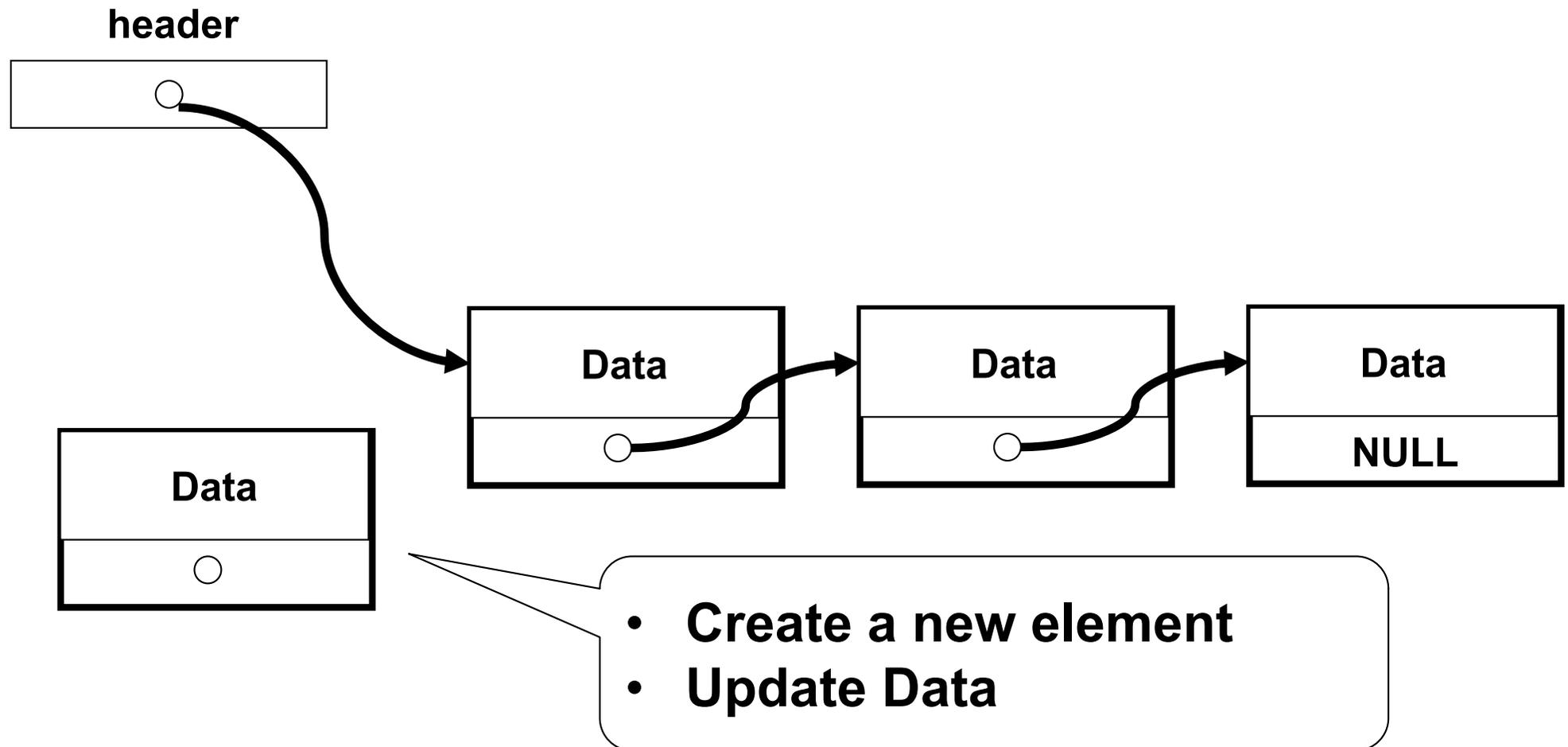
# ***Insert operations***

- Insert at the head***
- Insert inside***
- Insert at the end***

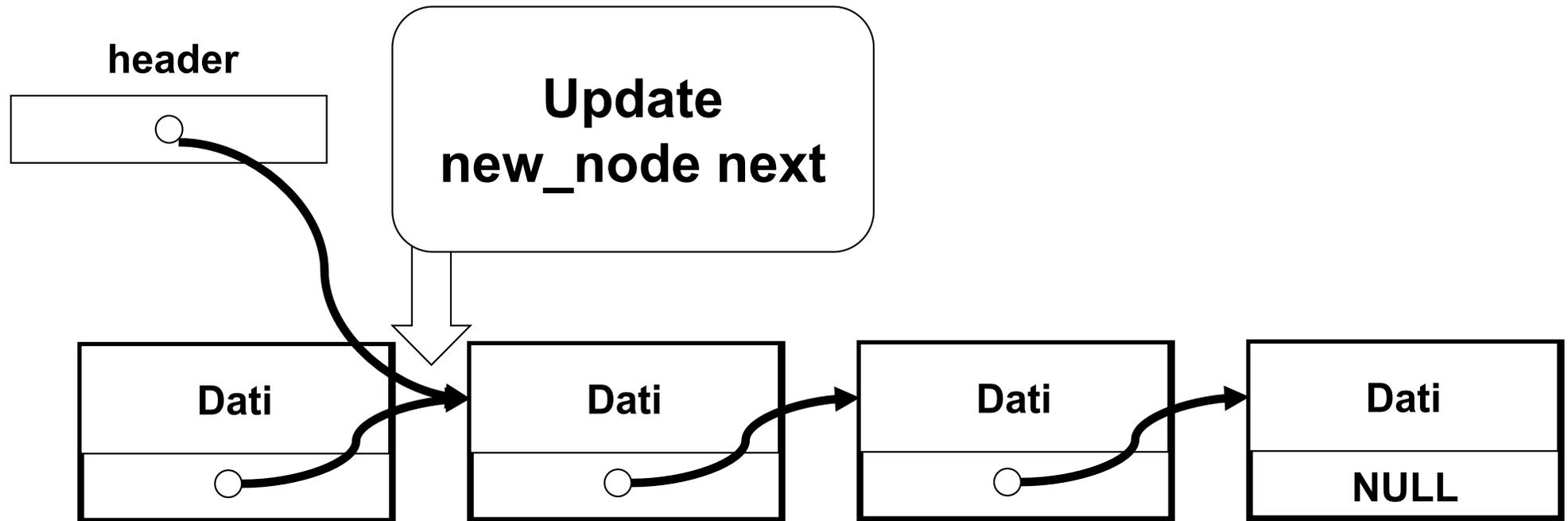
# *Insert at the head*



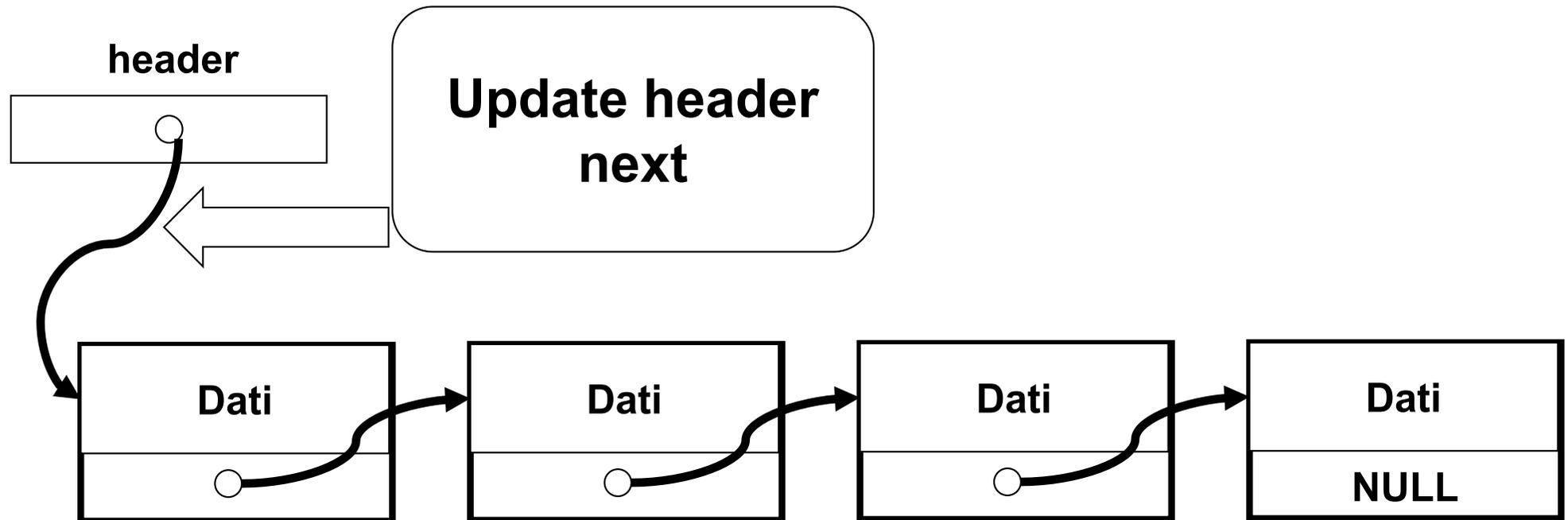
# *Insert at the head*



# *Insert at the head*



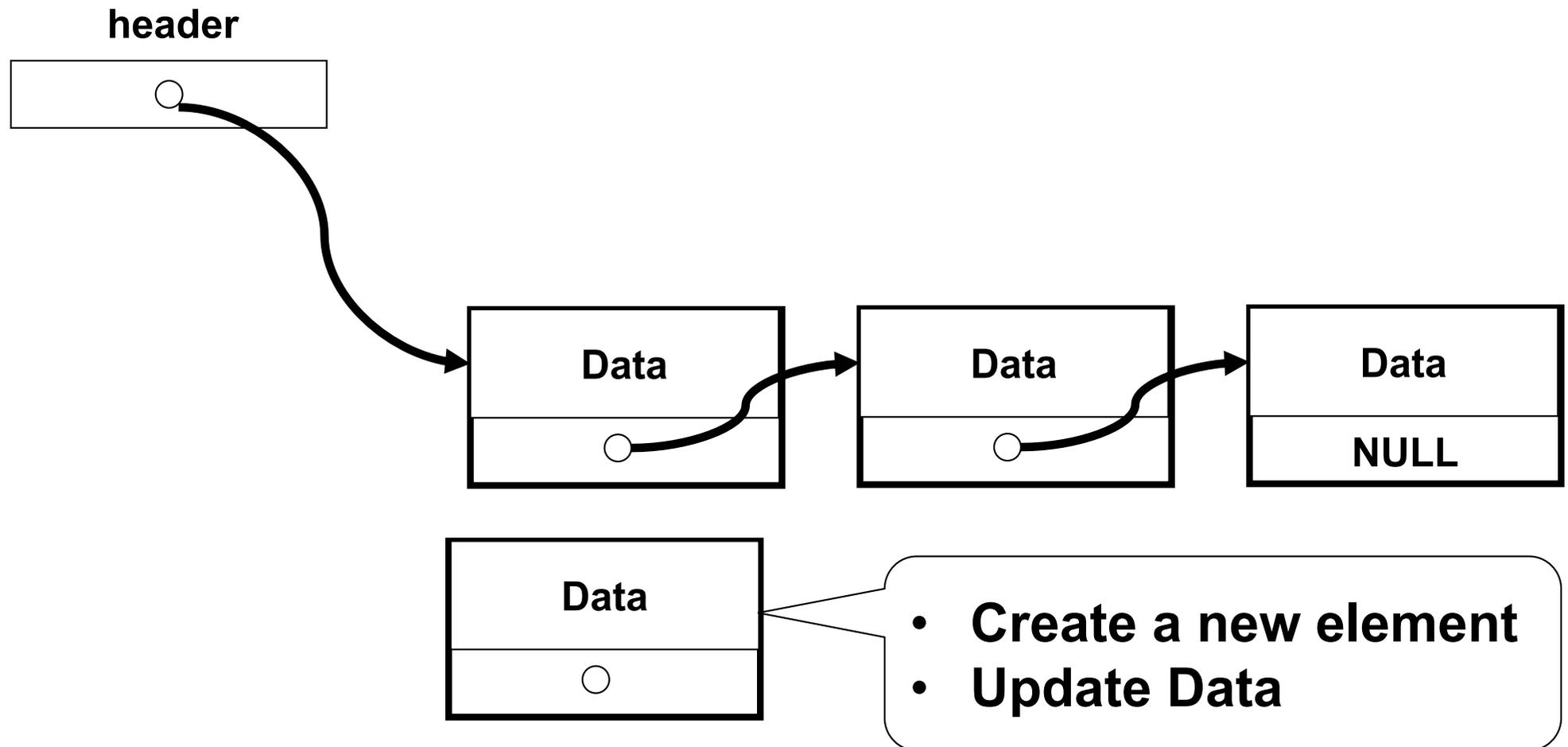
# *Insert at the head*



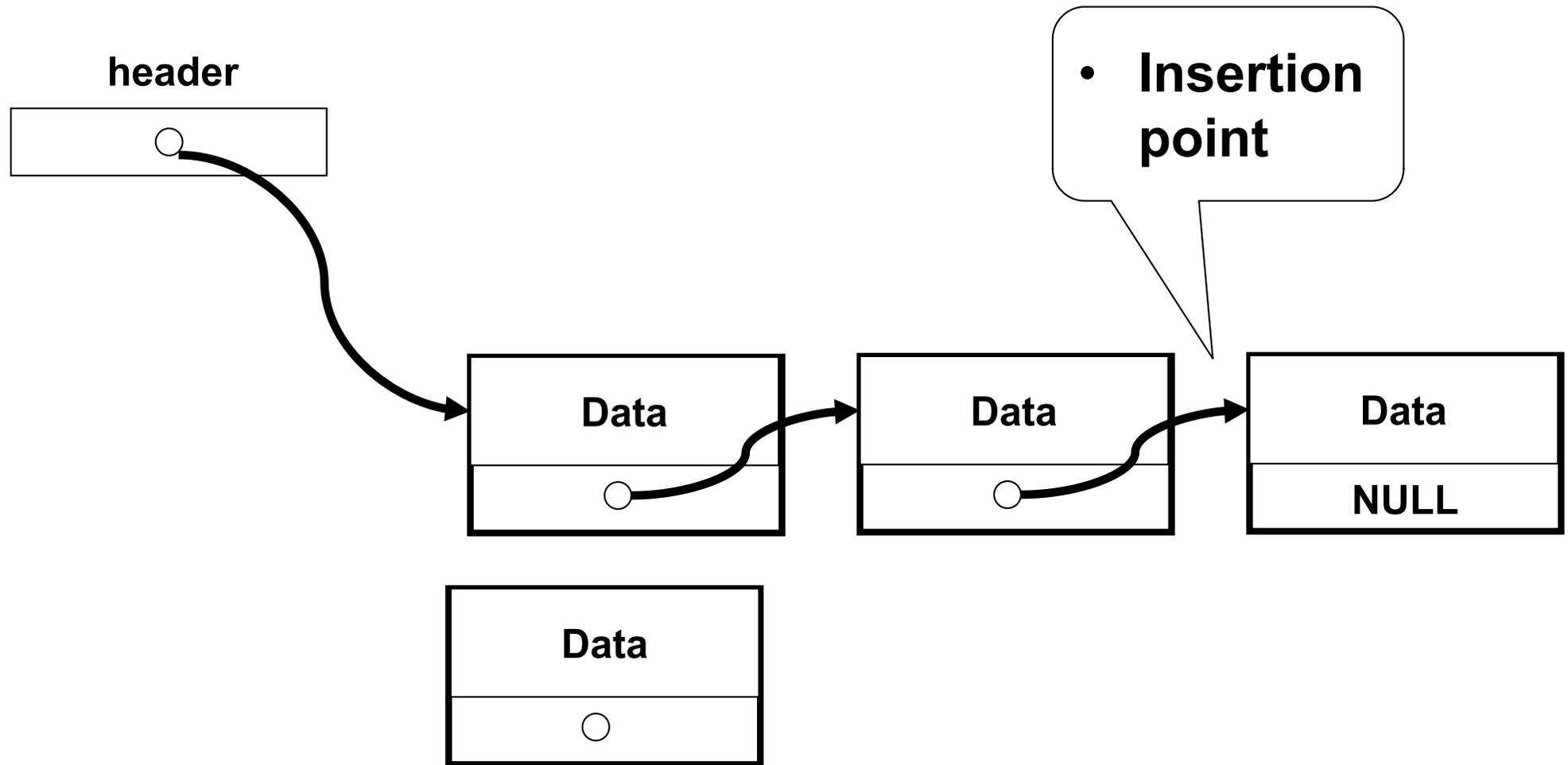
# ***Insert operations***

***– Insert inside***

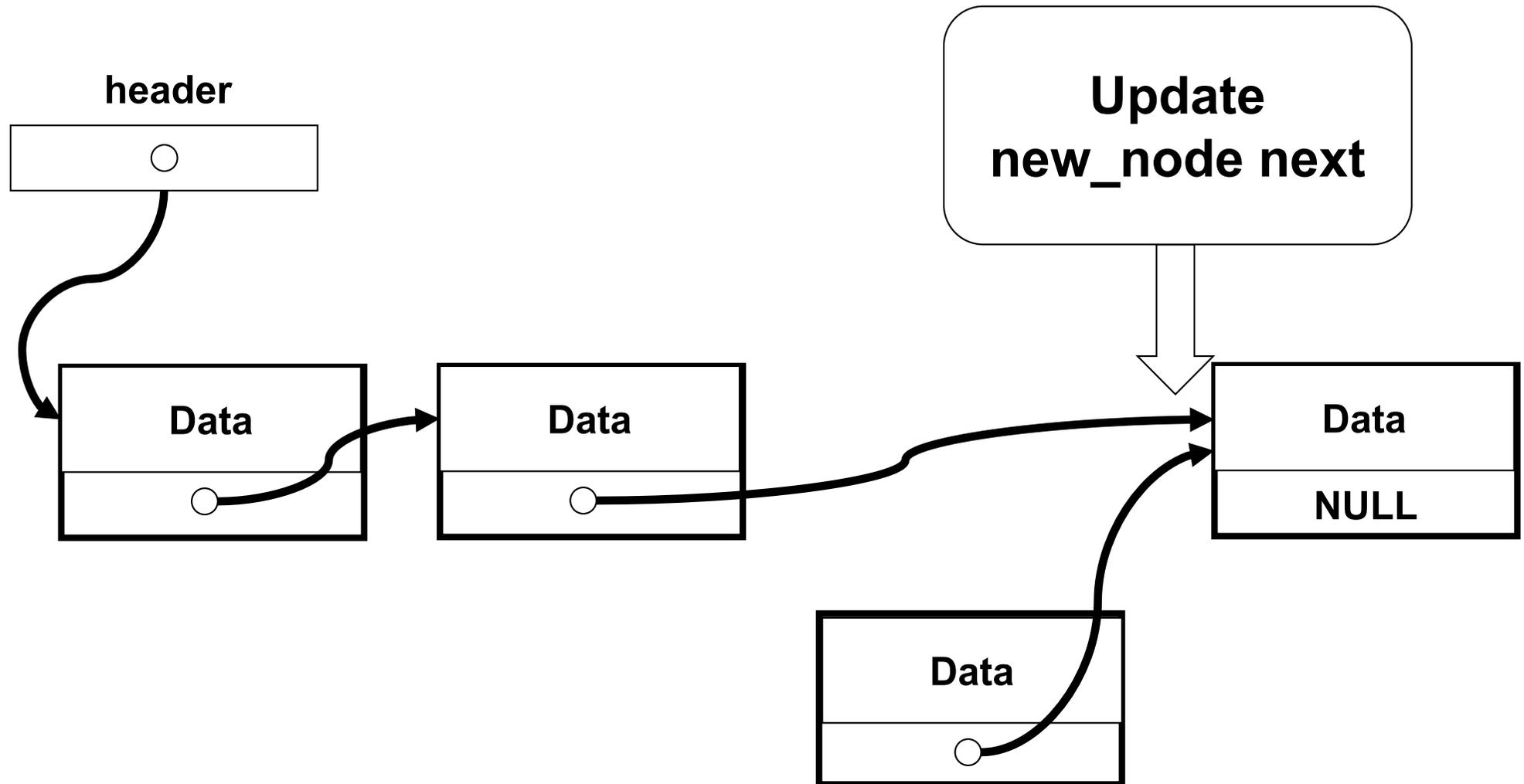
# *Insert inside*



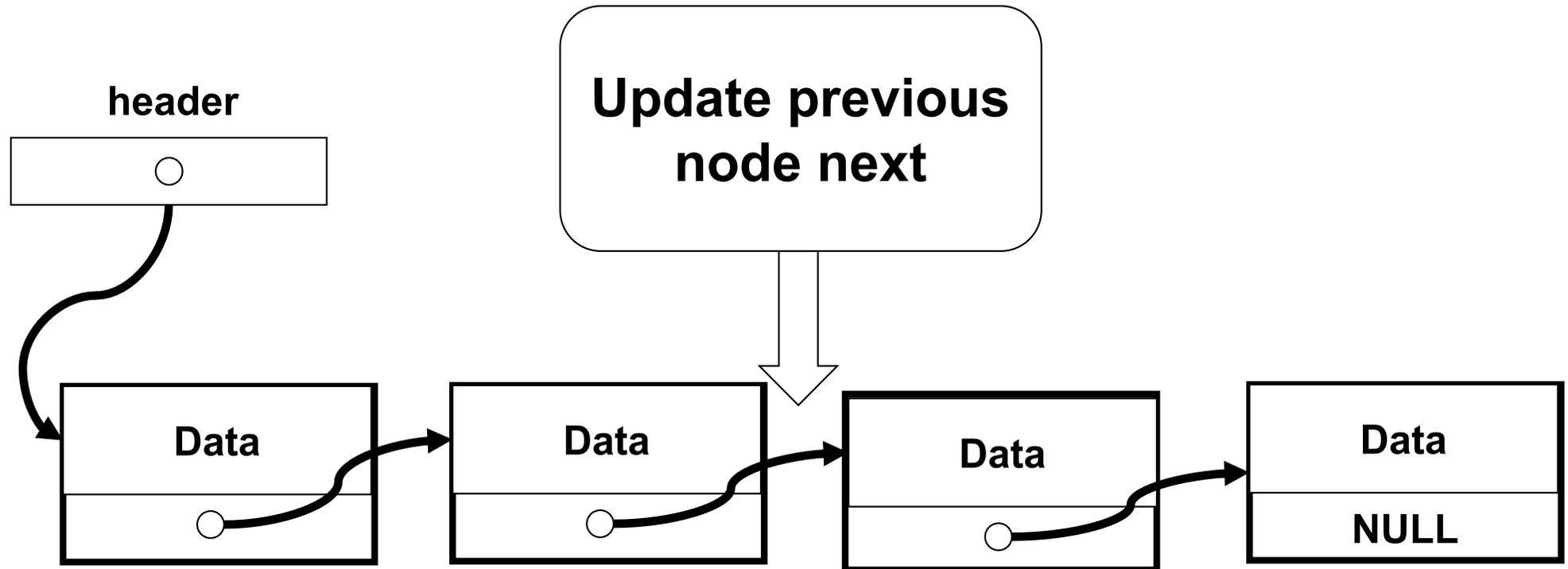
# *Insert inside*



# *Insert inside*



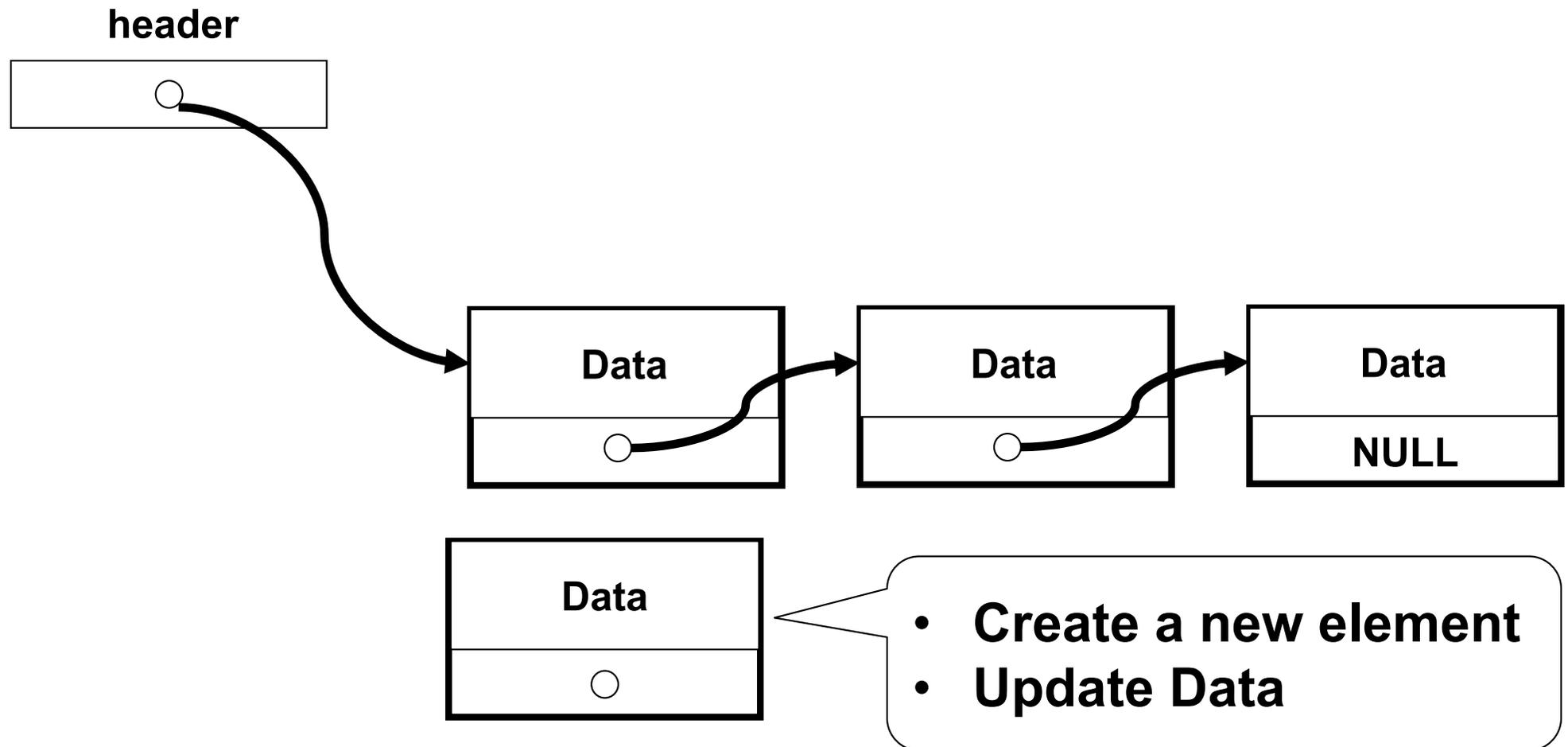
# *Insert inside*



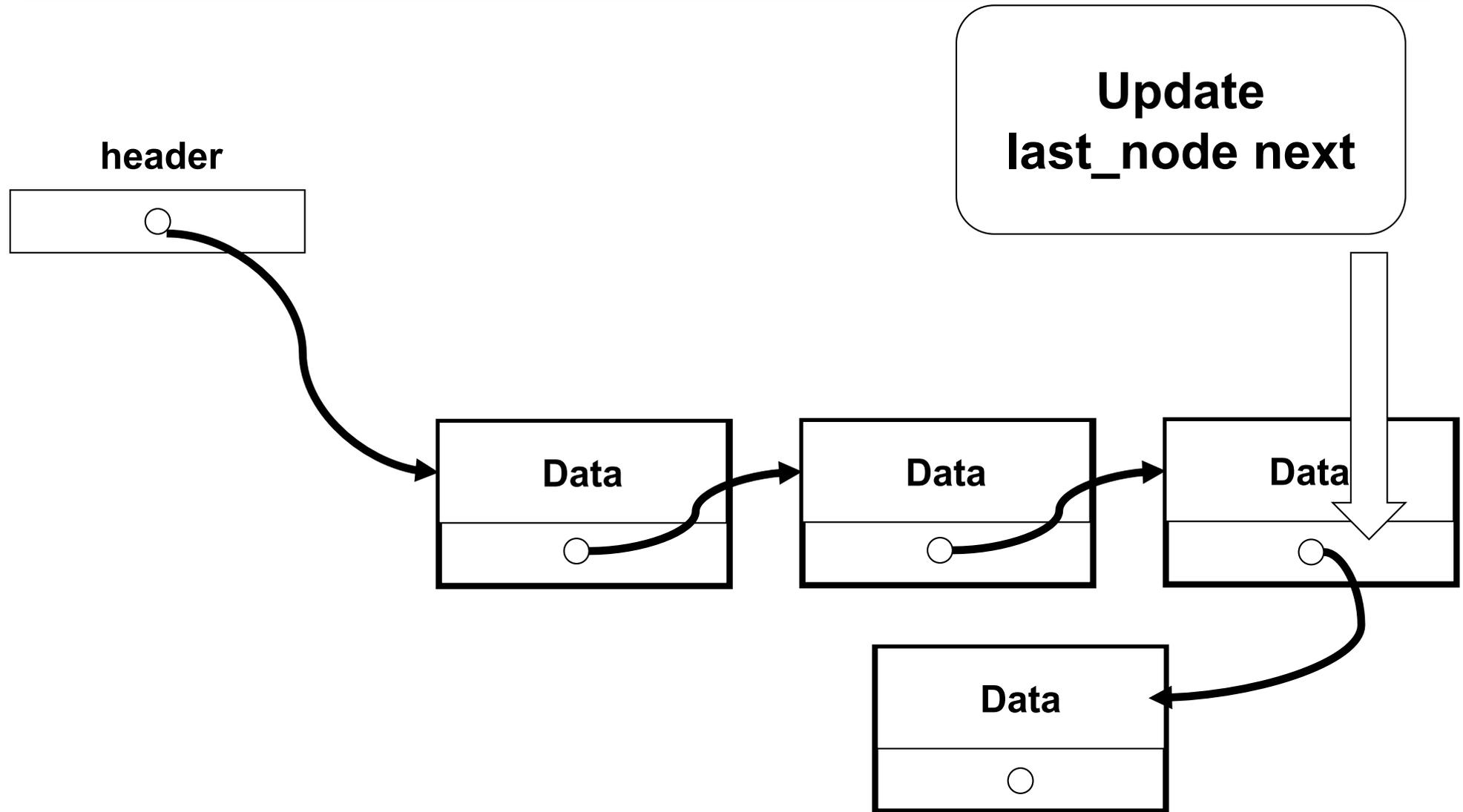
# ***Insert operations***

***– Insert at the end***

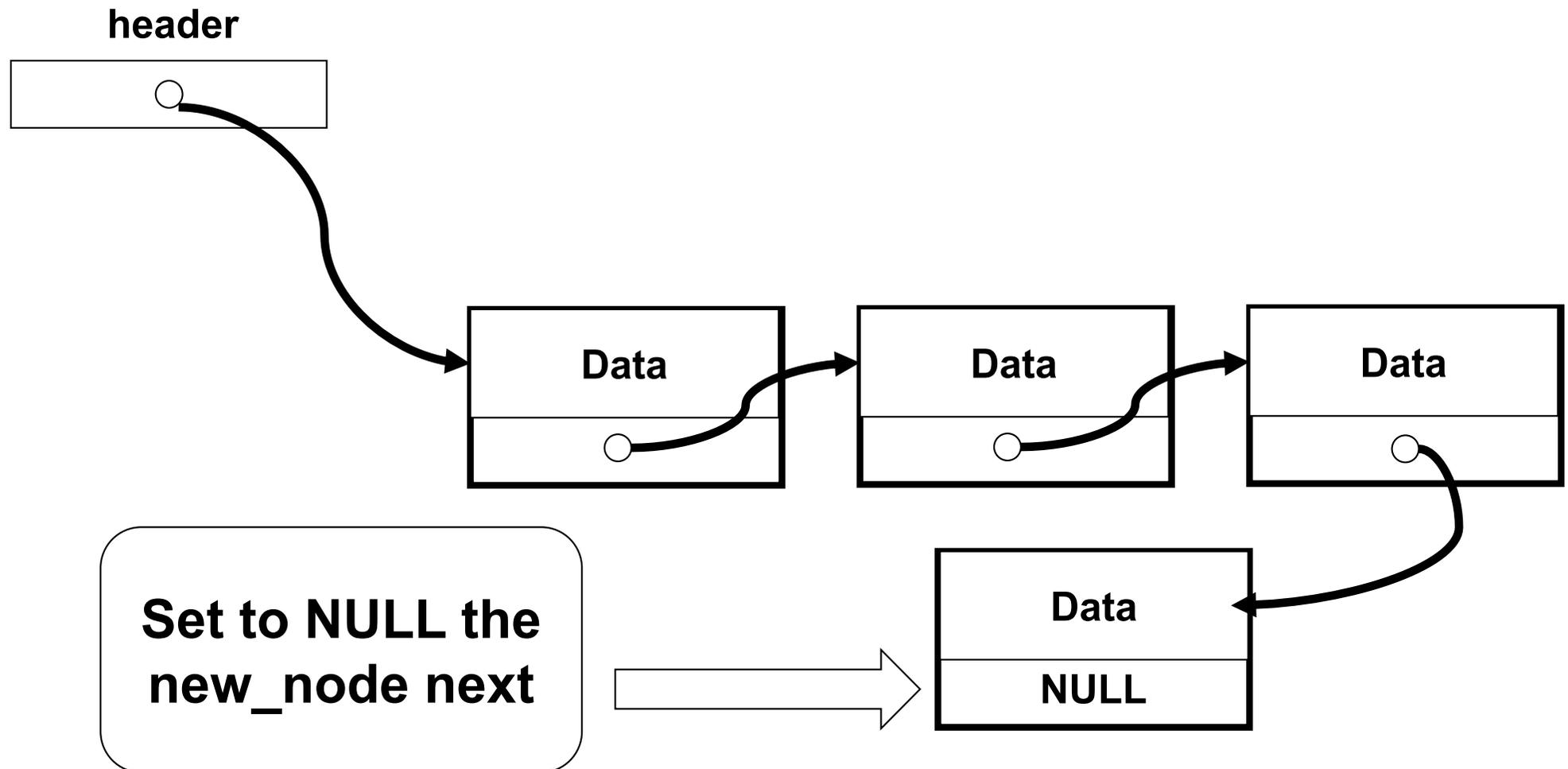
# *Insert at the end*



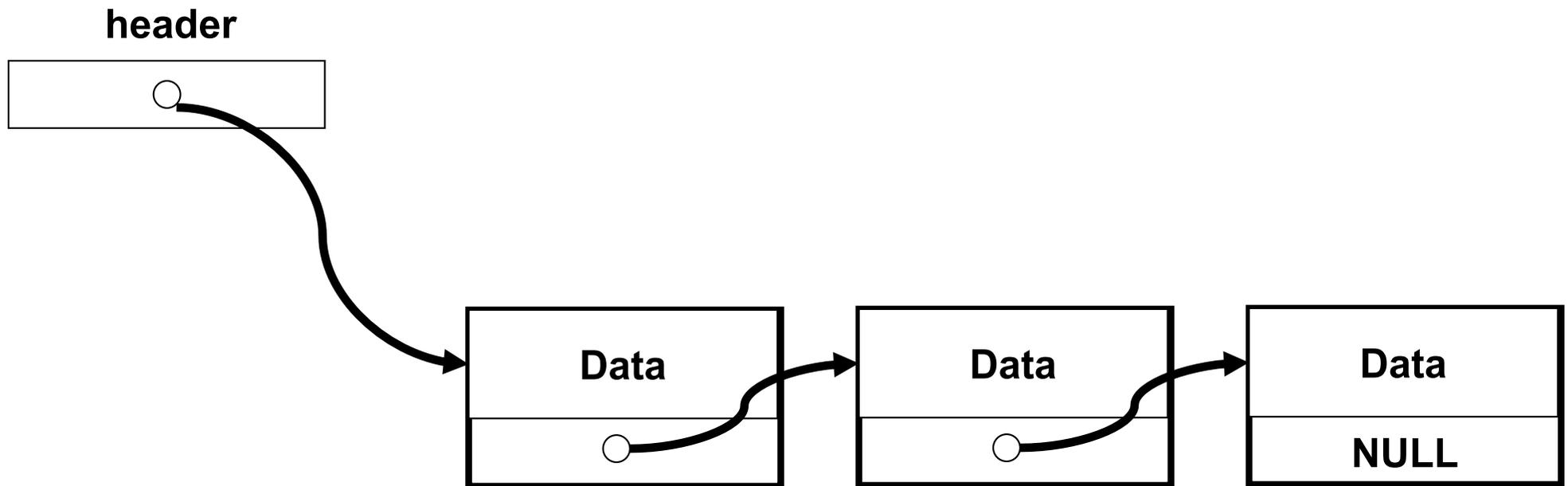
# *Insert at the end*



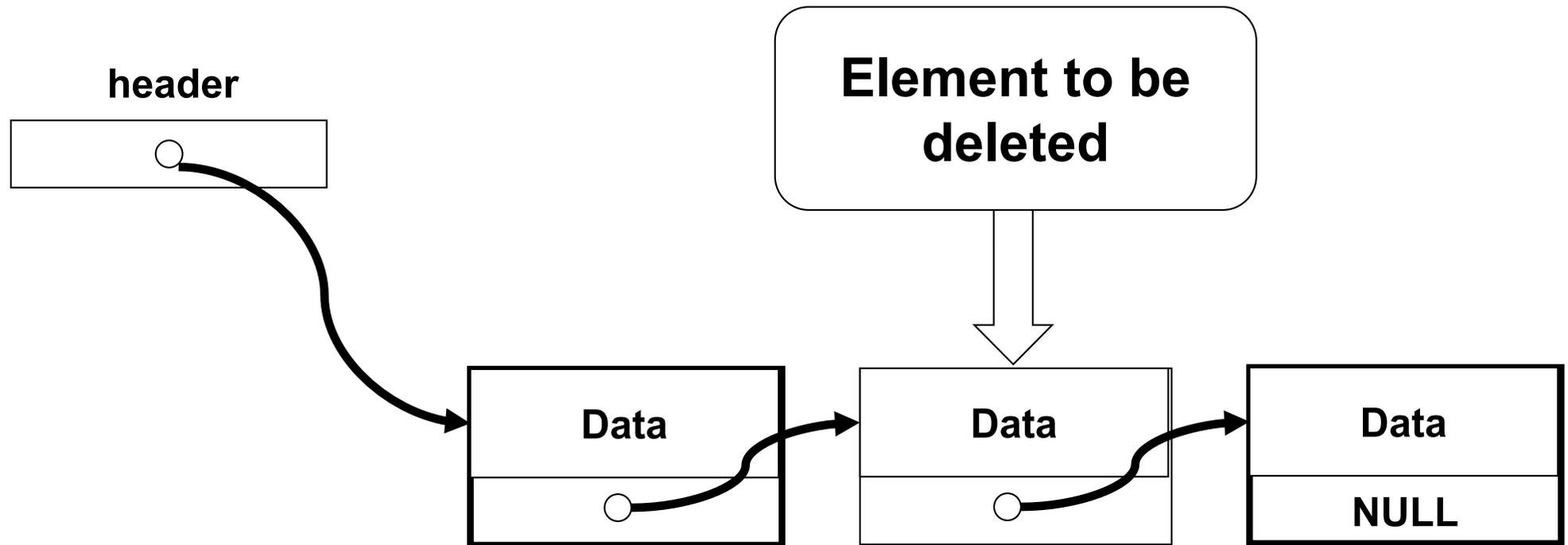
# *Insert at the end*



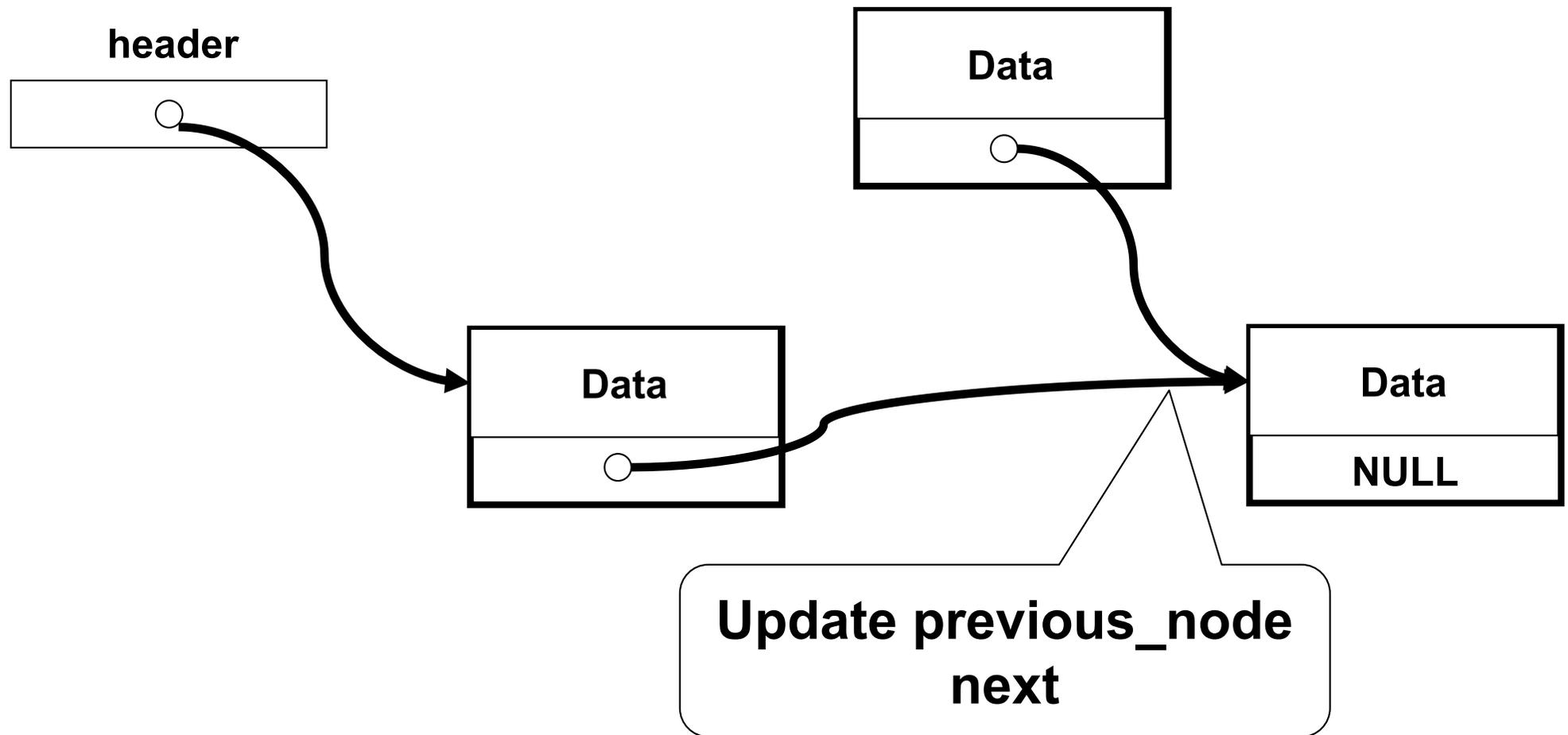
# Delete operation



# Delete operation

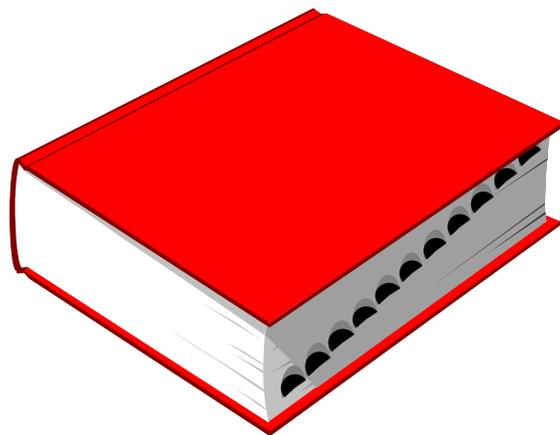


# Delete operation



# *Outline*

- Lists
- List operations
- List implementation
- Sentinels
- Doubly and multiple linked lists
- STL Lists



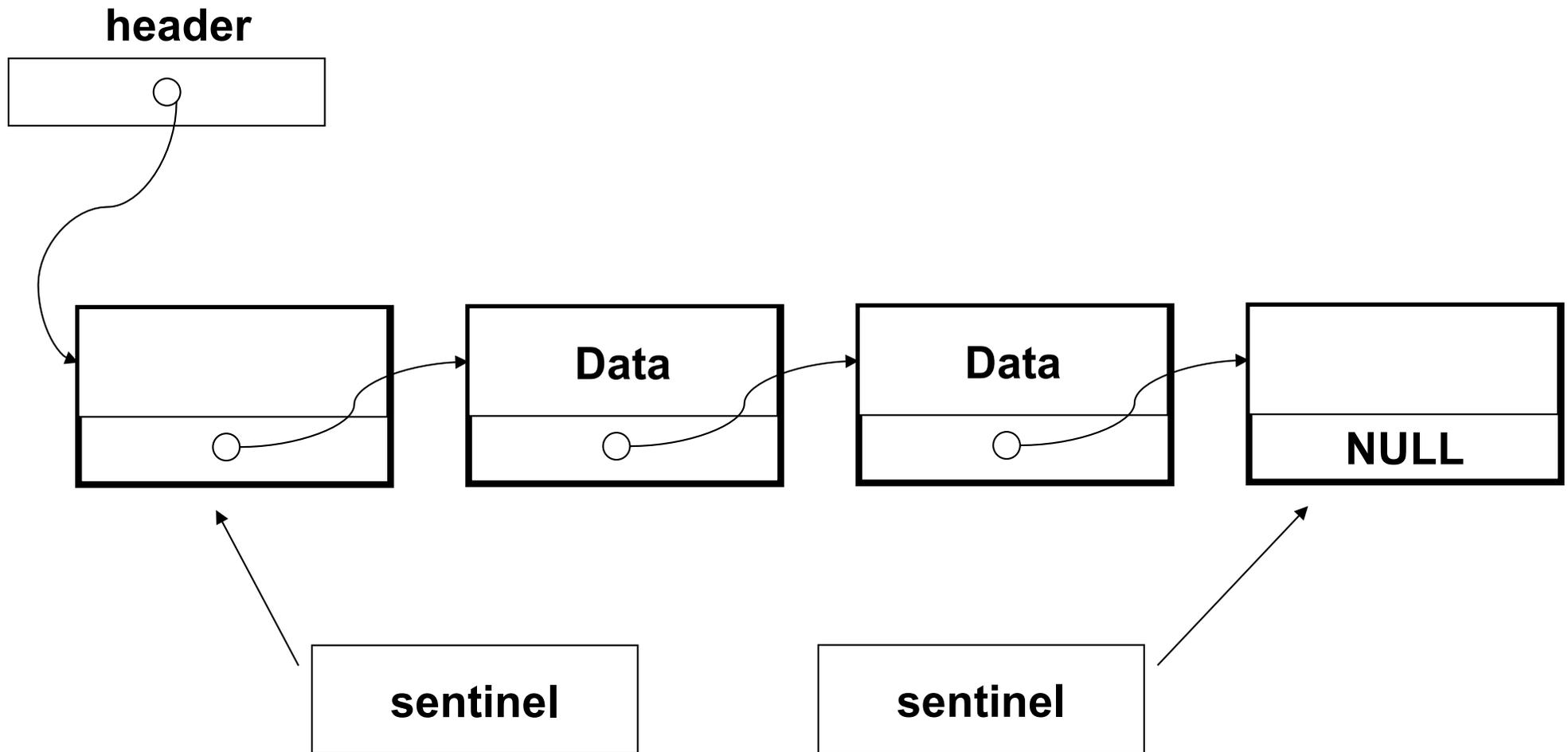
# ***Sentinels***

***Dummy elements  
added to the head  
and tail of a list.  
Sentinels simplify  
boundary conditions.***

# ***Sentinels***

- ***Head sentinels:***  
used to avoid header modification during a list insertion or deletion in the list header.
- ***Tail sentinels:***  
used to eliminate the second test during the search operations.

# Sentinels



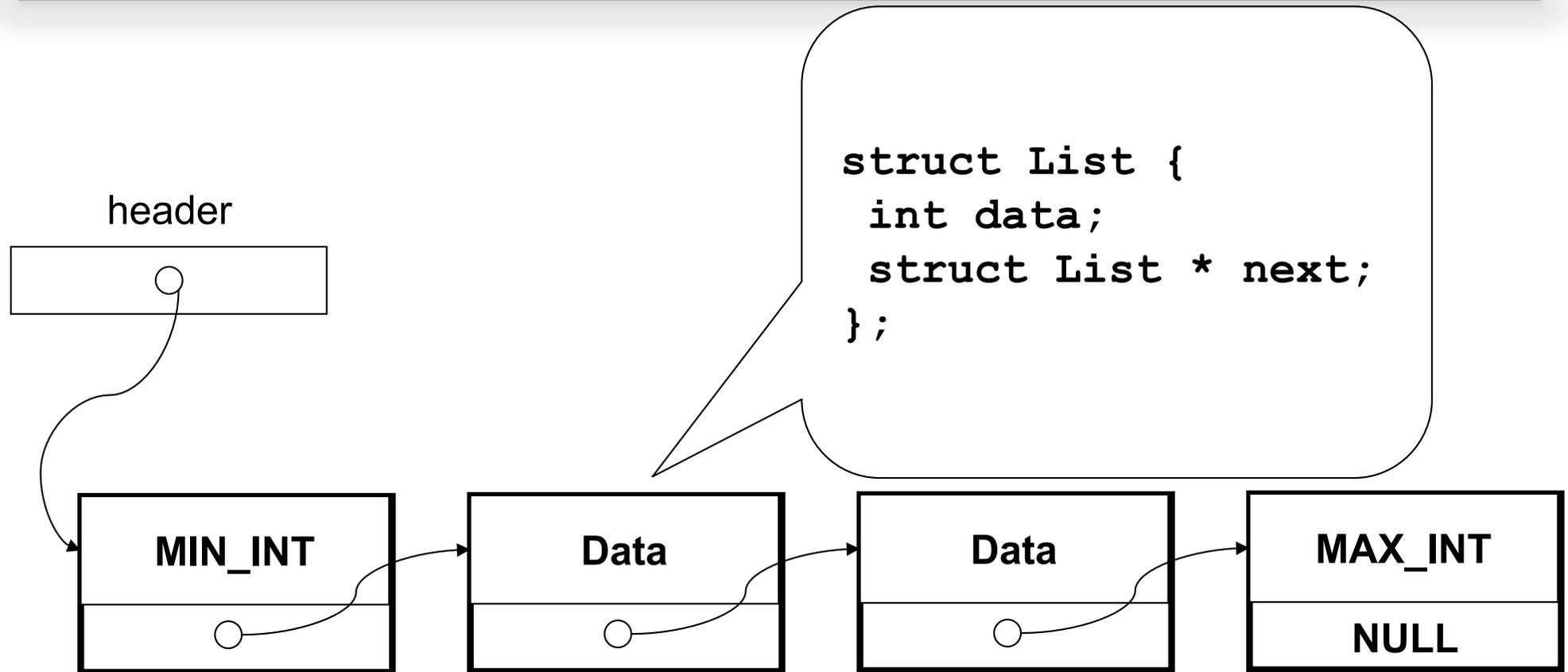
## ***Sentinels: unsorted lists***

- **Usually 2 sentinels are used, one in the head, the second one in the tail.**
- **Sentinels allow to reduce the code (i.e., it is not necessary to consider special cases for insert/delete in the head or tail).**

## ***Sentinels: sorted lists***

- **Usually 2 sentinels are used, one in the head, the second one in the tail containing the minimum and maximum values allowed in the list.**
- **Sentinels allow to simplify the code (i.e., it is not necessary to consider special cases for insert/delete in the head or tail).**
- **It is not necessary to test the end of the list.**

# Example



## ***Using the tail sentinel***

- **Searching in sorted lists:**
  - **The tail sentinel must contain the maximum value allowed.**
- **Searching in unsorted lists:**
  - **Saving into the tail sentinel the searched value. If the value is present, the search finds the actual node, otherwise, the last one.**

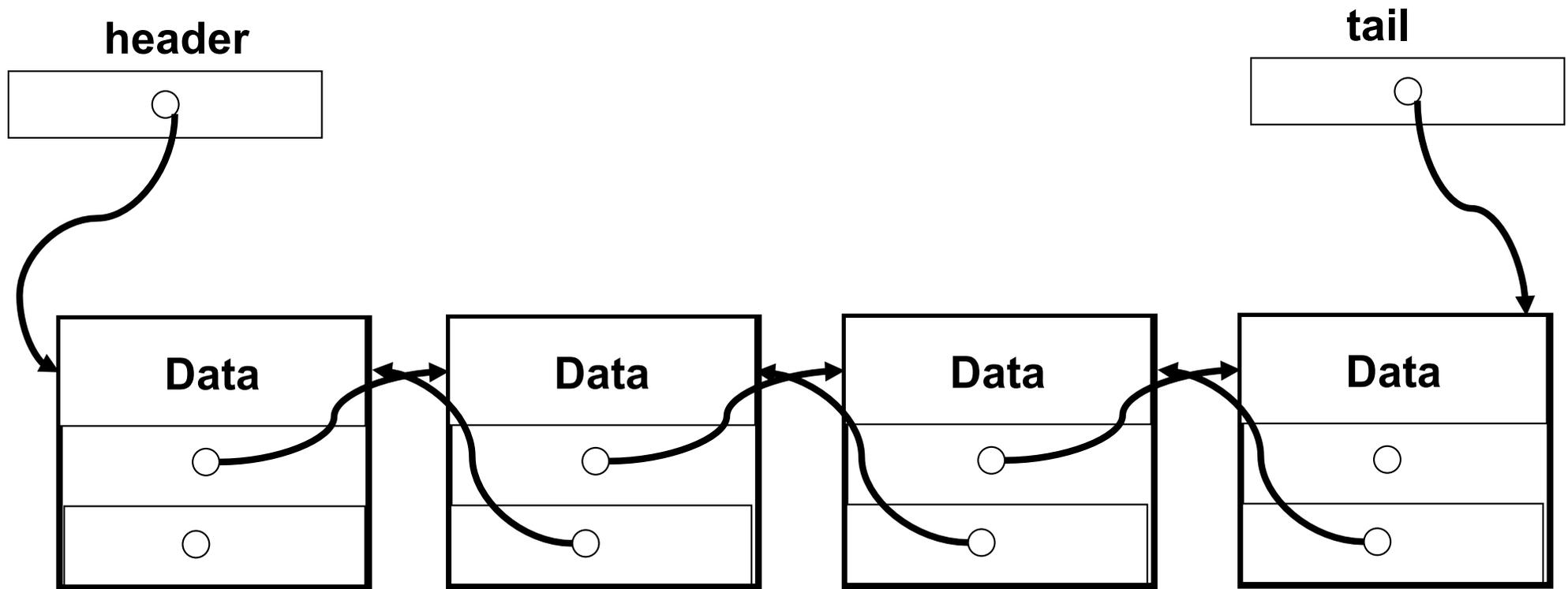
# ***Outline***

- **Lists**
- **List operations**
- **List implementation**
- **Sentinels**
- **Double and multiple linked lists**
- **STL Lists**

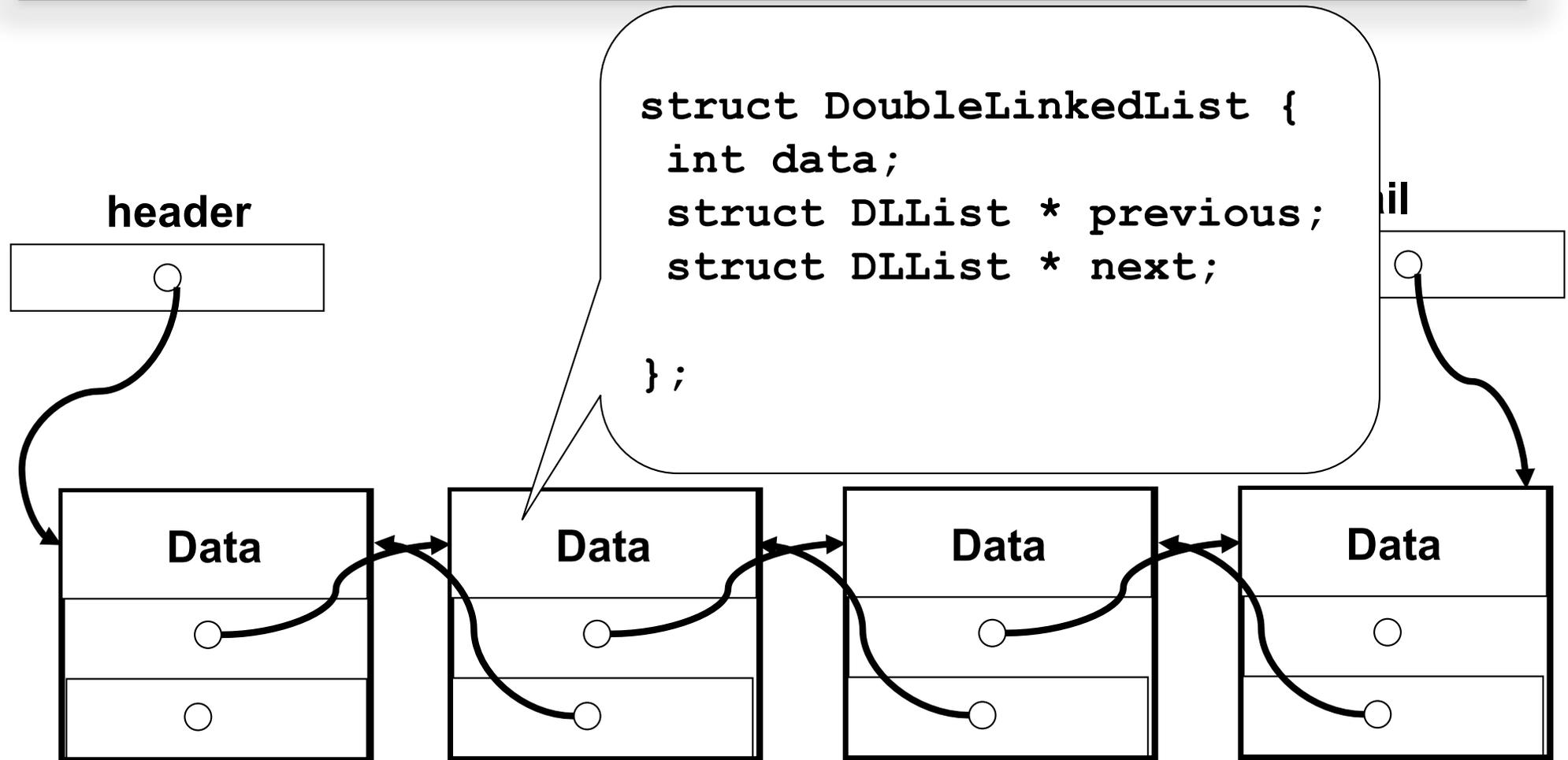
# ***Double and multiple linked lists***

- **In the cases when it is necessary to scan the list from the beginning to the end, and from the end to the beginning, it is ok to add a second pointer to every node.**
- **Two external pointers are required:**
  - **Header pointer**
  - **Tail pointer**

# *Double linked lists*

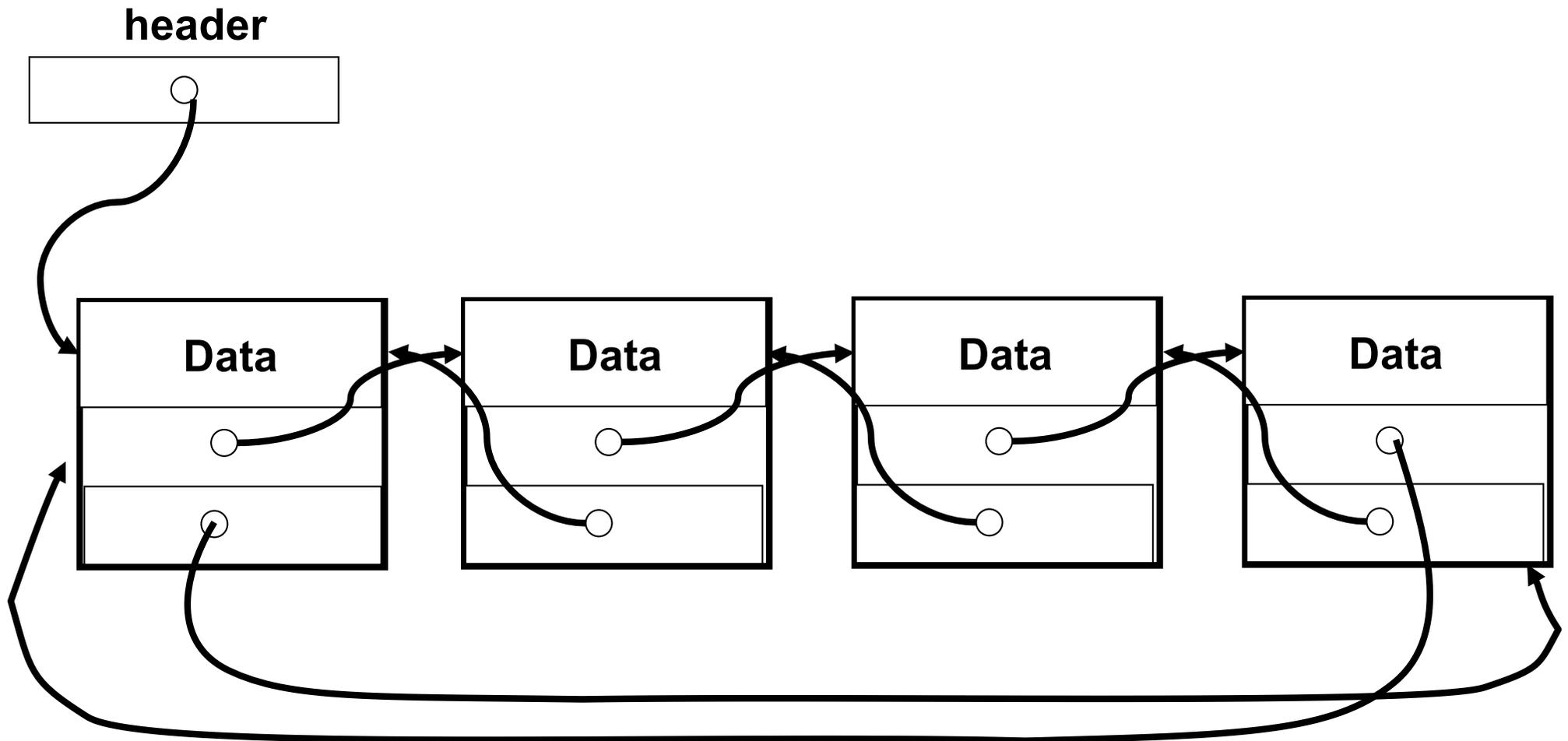


# Double linked lists



# Circular lists

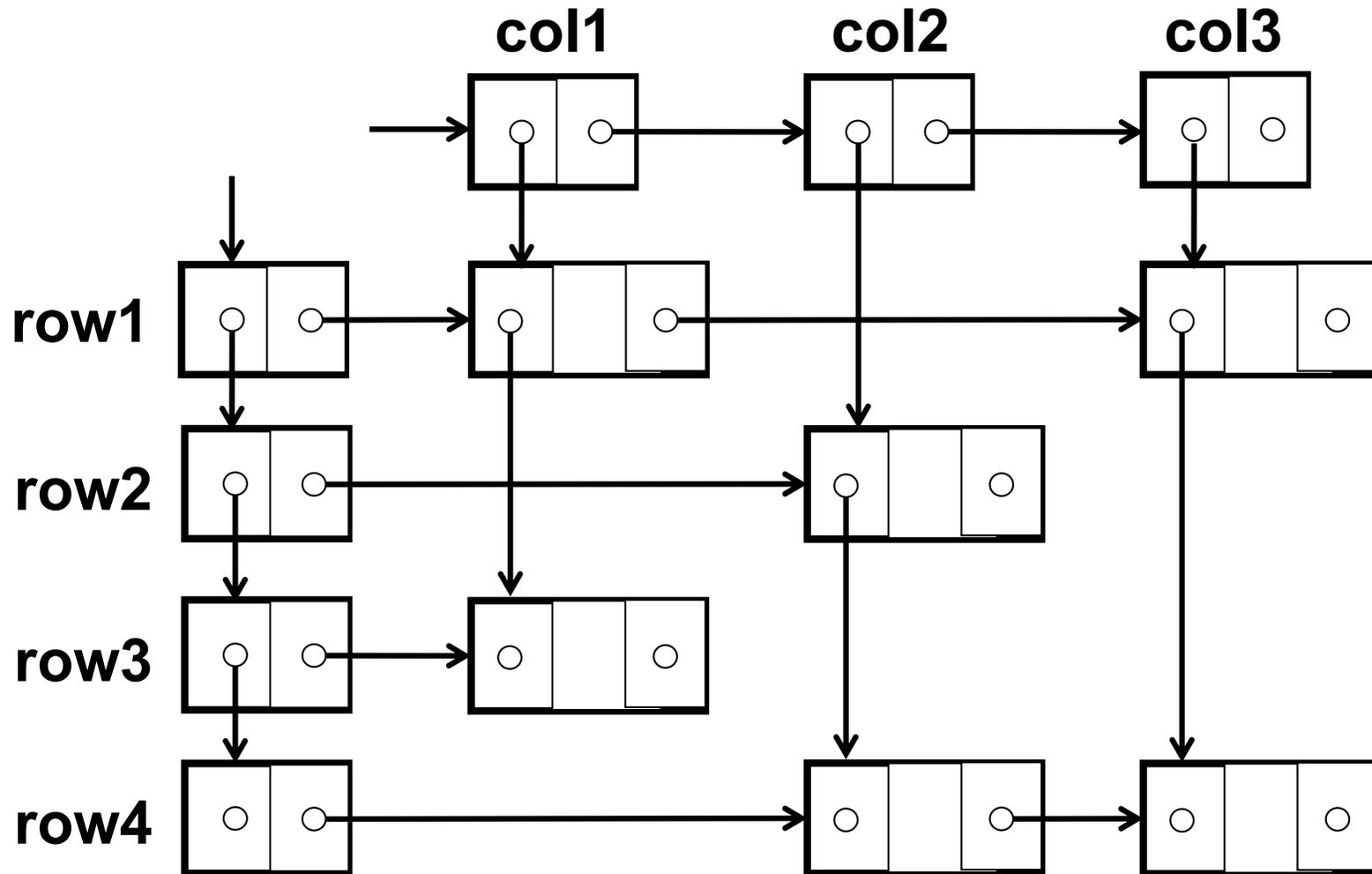
- The last node (tail) points to the first one (head).



# ***Multiple lists***

- **Every node in the list may point to several nodes.**

# Multiple lists



# *Outline*

- Lists
- List operations
- List implementation
- Sentinels
- Double and multiple linked lists
- STL Lists

# ***STL Lists***

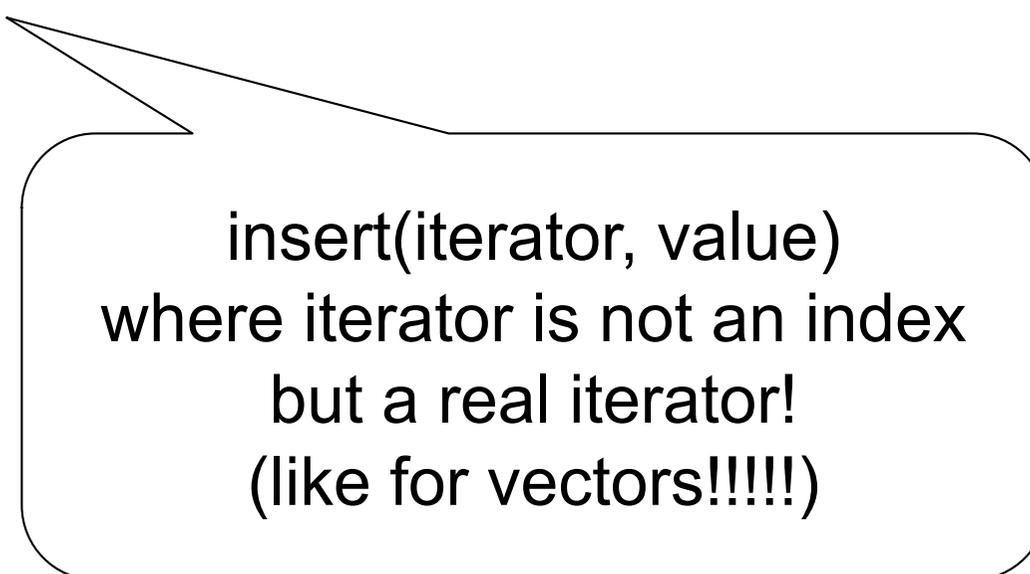
- **STL list container implements a double linked list**
  - **Iterator is a Bidirectional iterator**
- **C++ v11 introduced a (single) linked list container: `forward_list`**
  - **In this case, operations are allowed in one direction only... (better performances but less flexibility).**

# ***STL Lists - Insertion***

- **Like vectors:**
  - **push\_front**
  - **push\_back**
  - **insert**

# ***STL Lists - Insertion***

- **Like vectors:**
  - **push\_front**
  - **push\_back**
  - **insert**



insert(iterator, value)  
where iterator is not an index  
but a real iterator!  
(like for vectors!!!!)

# ***STL Lists - Deletion***

- **Like vectors:**
  - **pop\_front**
  - **pop\_back**
  - **erase**
  - **clear**
  - **remove**

# ***STL Lists - Deletion***

- **Like vectors:**
  - **pop\_front**
  - **pop\_back**
  - **erase**
  - **clear**
  - **remove**

erase(iterator position) → single element  
erase(iterator first, iterator last) → from a first to a last set of elements

# ***STL Lists - Deletion***

- **Like vectors:**
  - **pop\_front**
  - **pop\_back**
  - **erase**
  - **clear**
  - **remove**

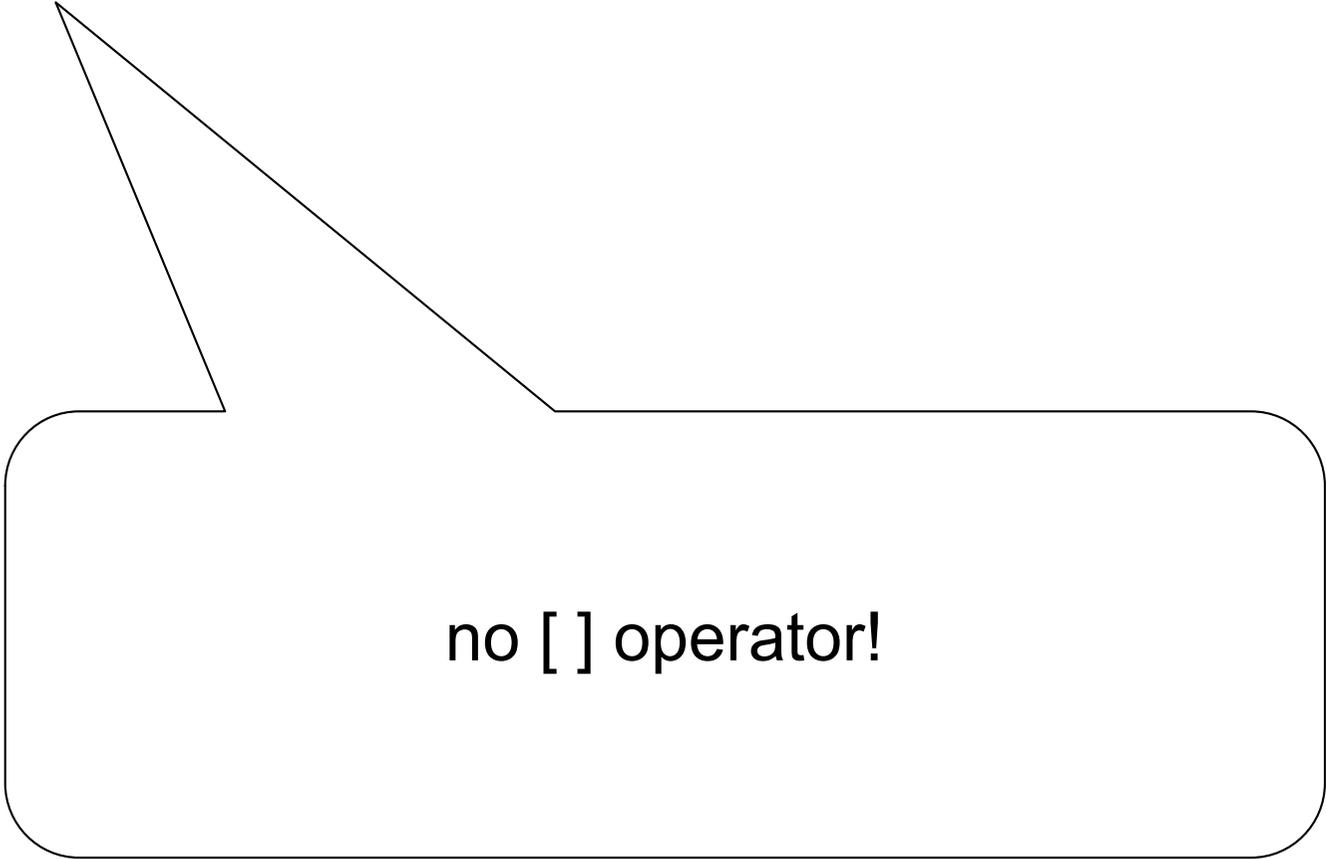
remove(value) → removes from the container all the elements that compare equal to value!

# ***STL Lists - Element access***

- **Like vectors:**
  - **front**
  - **back**

# ***STL Lists - Element access***

- **Like vectors:**
  - **front**
  - **back**



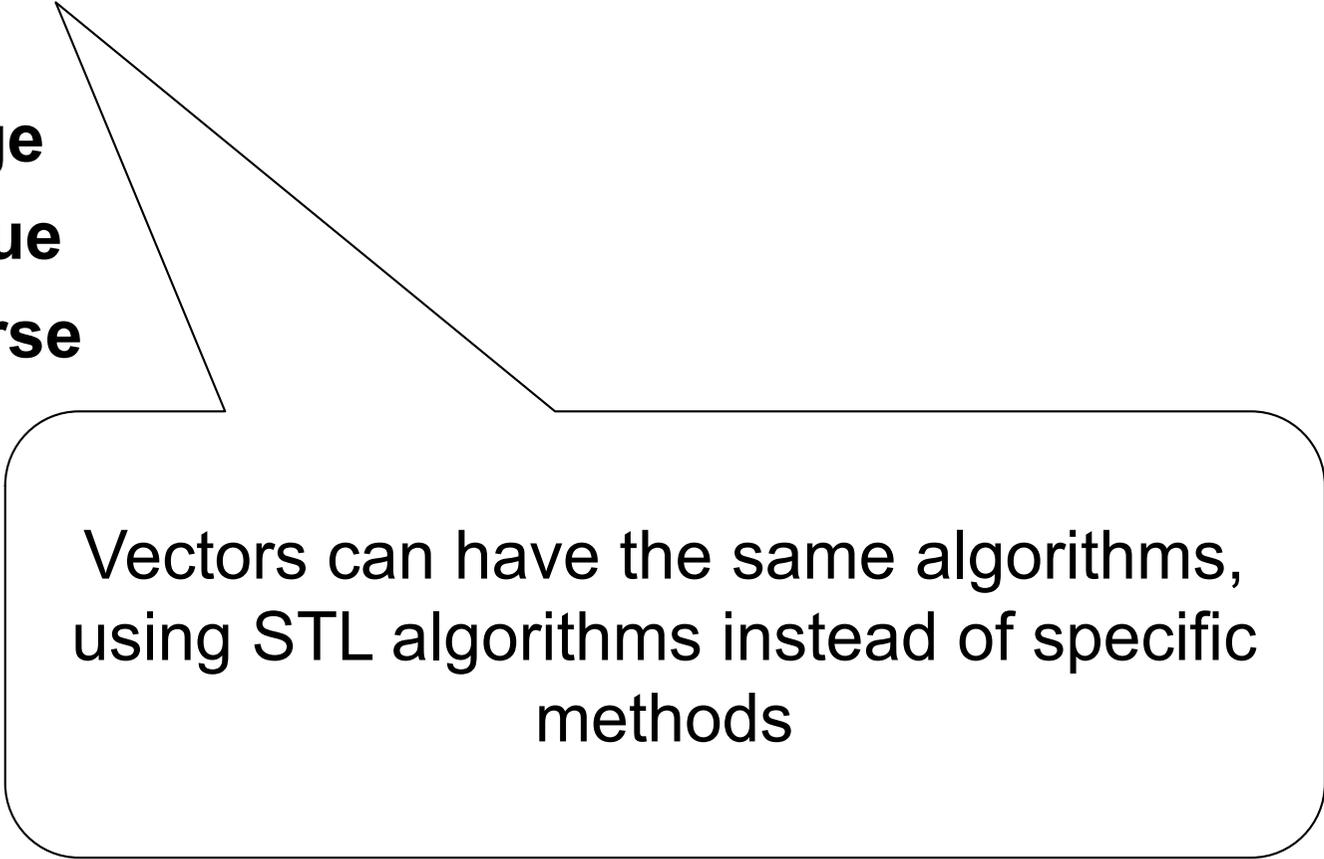
no [ ] operator!

# ***STL Lists - Specials***

- **Not-Like vectors:**
  - **sort**
  - **merge**
  - **unique**
  - **reverse**

# ***STL Lists - Specials***

- **Not-Like vectors:**
  - **sort**
  - **merge**
  - **unique**
  - **reverse**



Vectors can have the same algorithms,  
using STL algorithms instead of specific  
methods

# ***STL Lists - Specials***

- **Not-Like vectors:**
  - **sort**
    - . **sort elements by means of a function for the single element comparison you must provide!**
  - **merge**
  - **unique**
  - **reverse**

# ***STL Lists - Specials***

- **Not-Like vectors:**
  - **sort**
  - **merge**
    - . **merge a list into another one (the one you pass as parameter into the one you called the method from)**
      - **this clear the one you passed.**
    - . **overridden with a second version that accept a comparison function too.**
  - **unique**
  - **reverse**

# ***STL Lists - Specials***

- **Not-Like vectors:**
  - **sort**
  - **merge**
  - **unique**
    - **removes duplicates**
  - **reverse**

# ***STL Lists - Specials***

- **Not-Like vectors:**
  - **sort**
  - **merge**
  - **unique**
  - **reverse**
    - . **reverse the list!**

# References

- **A.V. Aho, J.E. Hopcroft, J.D. Ullman:**  
**“Data Structures and Algorithms,”**  
**Addison Wesley, Reading MA (USA), 1983**  
**pp 37-74**
- **J. Esakow. T. Weiss**  
**“Data structure: an advanced approach using C,”**  
**Prentice Hall, Englewood Cliffs NJ (USA), 1982**  
**pp 54-237**
- **C.J. Van Wyk:**  
**“Data Structures and C Programs,” Addison**  
**Wesley, Reading MA (USA), 1988**  
**pp 49-128**

# References

- **R. Sedgewick:**  
**“Algorithms in C,”**  
**Addison Wesley, Reading MA (USA), 1990**  
**pp 15-34**
- **E. Horowitz, S. Sahni:**  
**“Fundamentals of Computer Algorithms,”**  
**Pittman, London (UK), 1978**  
**pp 65-202**
- **N. Wirth:**  
**“Algorithms + Data Structures = Programs,”**  
**Prentice Hall, Englewood Cliffs NJ (USA), 1976**  
**pp 162-188**

Малые Автюхи, Калининский район, Республики Беларусь

